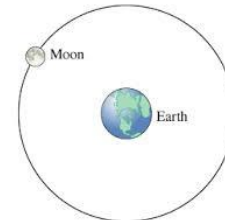


# Orbital Motion and Tides

## Mutual Gravitation

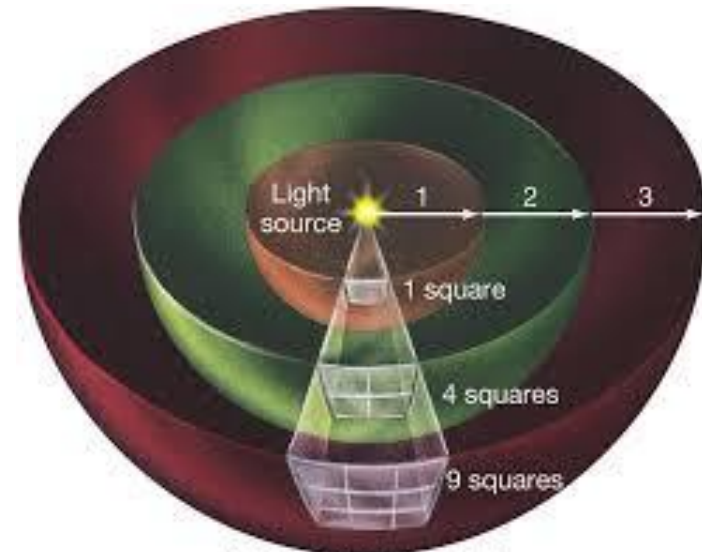
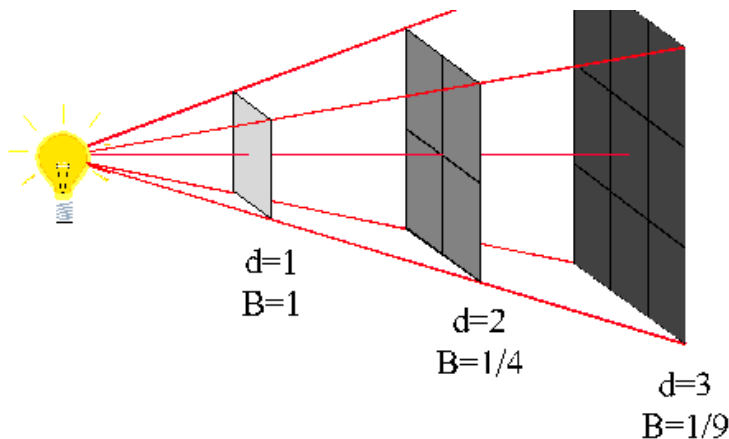
- ▶ Once \_\_\_\_\_ figured out his laws, he was able to better understand \_\_\_\_\_
  - 1<sup>st</sup> and 2<sup>nd</sup> law – bodies \_\_\_\_\_ downward because some force must be pulling \_\_\_\_\_ on them
    - Ex: the Moon orbiting the Earth
      - It has to be pulled by something and motion along a curved path is *accelerated motion* which is required by a force causing it to follow that curved path
- ▶ Newton anticipated that the same \_\_\_\_\_ holding the Moon in orbit was the same as \_\_\_\_\_ here on Earth, but that it might get weaker as it reached outer space



# Orbital Motion and Tides

## Mutual Gravitation

- ▶ **Inverse Square Law** – strength of a \_\_\_\_\_ will \_\_\_\_\_ as the square of the \_\_\_\_\_ increases
  - Saw this with light
    - A screen set up 1 meter away from a candle flame received a certain amount of light and then that light covered 4 sq. meters when the screen was 2 meters away
    - The light intensity was inversely proportional to the square distance of the screen



# Orbital Motion and Tides

## Mutual Gravitation

- ▶ Earth's gravity follows the inverse \_\_\_\_\_ law according to Newton
  - This includes the distance from the Earth's \_\_\_\_\_ and not surface
  - Ex: the Moon is 60 Earth radii away  
gravity is  $60^2$  (or 360)x less than at the Earth's surface  
acceleration at Earth's surface is  $9.8 \text{ m/s}^2$   
this estimates out to be . \_\_\_\_\_  $\text{m/s}^2$

To keep the Moon in orbit, acceleration = . \_\_\_\_\_  $\text{m/s}^2$

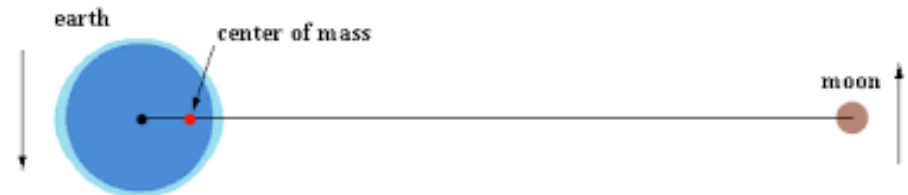


Figure 2. Moon's gravitational pull plus 2-body rotation

# Orbital Motion and Tides

## Mutual Gravitation

- ▶ Gravity depends on \_\_\_\_\_, and with Earth's mass being so substantial, it's strong enough to hold the \_\_\_\_\_ in orbit

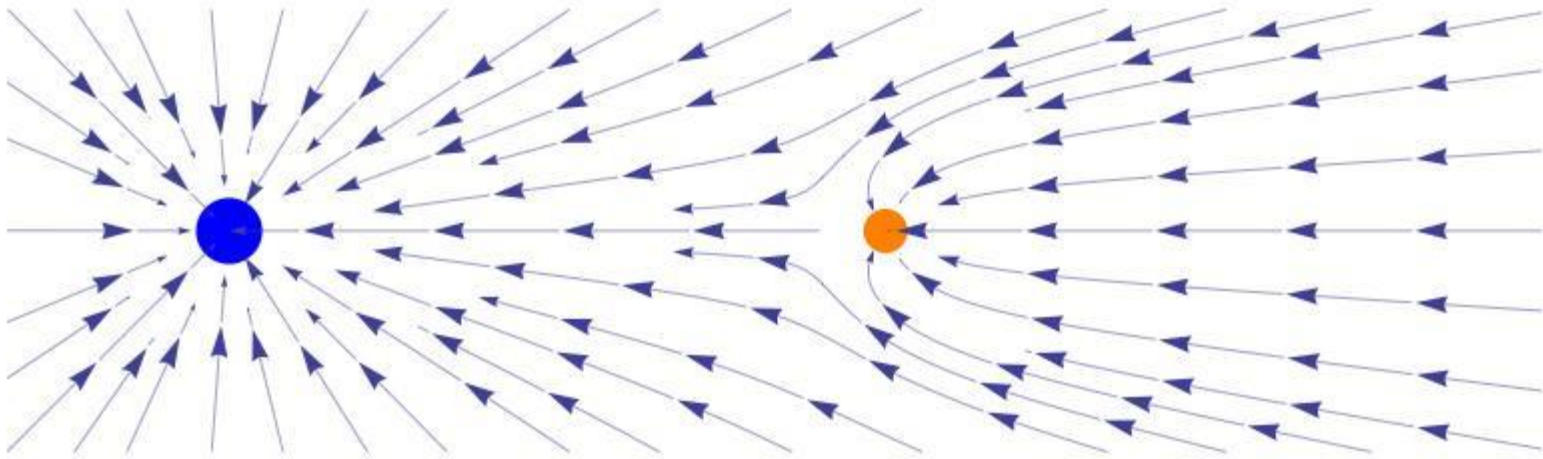
$$F = -\frac{Gm_1m_2}{r^2}$$

- $F$  – \_\_\_\_\_
  - $G$  – gravitational constant
  - $r$  – \_\_\_\_\_ between the masses
  - $m_1$  – mass of the object 1
  - $m_2$  – mass of object 2
- ▶ The force of gravitational attraction between two masses ( $m_1$  and  $m_2$ ) is proportional to the product of the masses and inversely proportional to the square of the distance between them

# Orbital Motion and Tides

## Mutual Gravitation

- ▶ **Field** – When two objects exert \_\_\_\_\_ onto each other without physically \_\_\_\_\_
  - Ex: Earth and the Moon
  - Used to describe gravity that follows the inverse \_\_\_\_\_ law



# Orbital Motion and Tides

## Orbits

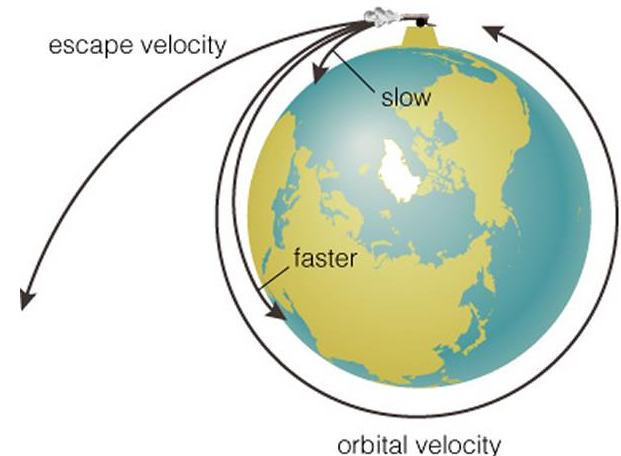
- ▶ Orbital motion is how gravity pulls on an \_\_\_\_\_ object
  - Tidal motion is how gravity pulls on \_\_\_\_\_ of an object
- ▶ \_\_\_\_\_ was the first to figure out that objects which are orbiting are technically “falling”

# Orbital Motion and Tides

## Orbits

### ▶ Orbiting Earth:

1. An object orbiting Earth is actually falling towards Earth's \_\_\_\_\_
  - It misses each time because of orbital velocity
  - **Circular Velocity** – the velocity needed to stay in a \_\_\_\_\_ orbit
  - Just above Earth's atmosphere, circular velocity is about 7780 m/s (17,400 mph) with an orbital period of about 90 minutes

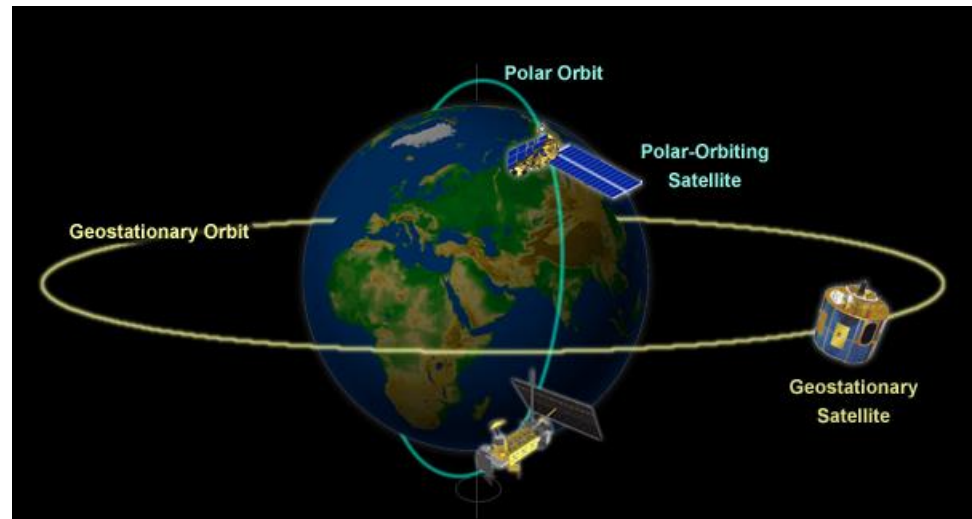


# Orbital Motion and Tides

## Orbits

### ▶ Orbiting Earth:

1. An object orbiting Earth is actually falling towards Earth's center
  - **Geosynchronous Satellites** – satellites that orbit \_\_\_\_\_ with the rotation of Earth and remain above a fixed \_\_\_\_\_
    - About 42,230 km (26,240 mi) from Earth's center
    - Orbits in 24 hours





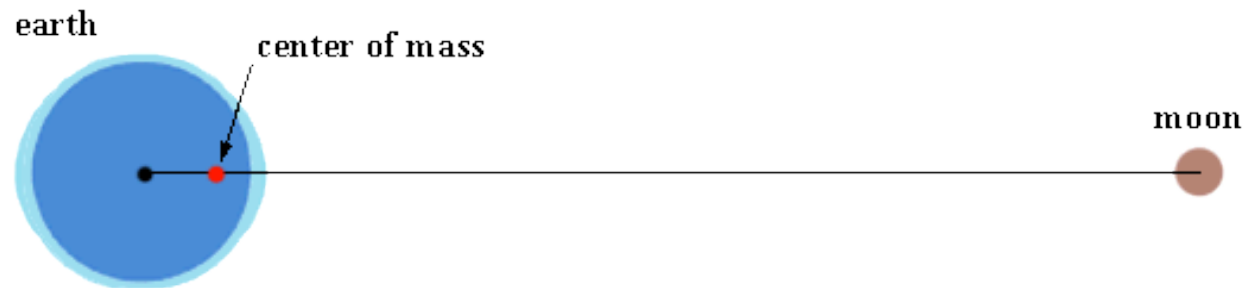
# Orbital Motion and Tides

## Orbits

### ▶ Orbiting Earth:

2. Objects that are orbiting each other actually revolve around their mutual center of mass

- An object doesn't orbit Earth, but rather, they orbit each \_\_\_\_\_
  - Remember, gravity is mutual
- **Center of Mass** – the \_\_\_\_\_ point of the gravitational system (or two objects)
- Because of Earth's enormous mass, "they" orbit \_\_\_\_\_ to Earth



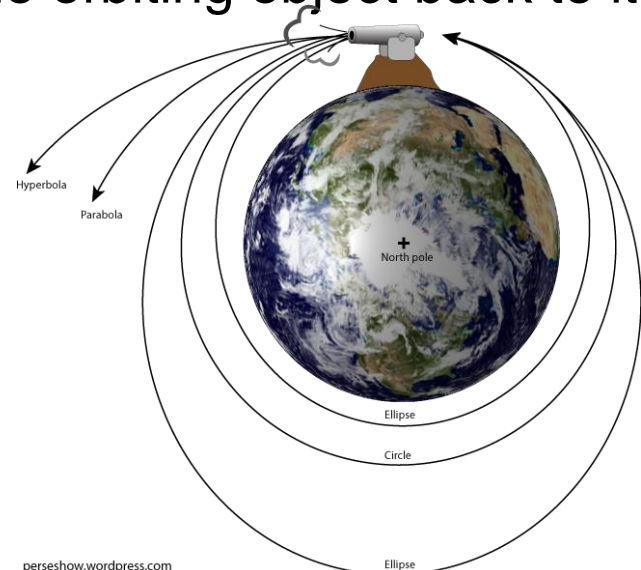
# Orbital Motion and Tides

## Orbits

### ▶ Orbiting Earth:

3. There are closed and open orbits. A certain *escape* \_\_\_\_\_ is needed to leave Earth

- **Closed Orbit** – \_\_\_\_\_ the orbiting object to its original starting point
- **Escape Velocity** – ( $V_e$ ) the velocity needed to \_\_\_\_\_ a body
- **Open Orbit** – does not \_\_\_\_\_ the orbiting object back to its original starting point



# Orbital Motion and Tides

## Orbital Velocity

- ▶ **Circular Velocity** – velocity an object must have in a \_\_\_\_\_ direction to remain in a \_\_\_\_\_ orbit

$$V_c = \sqrt{\frac{GM}{r}}$$

- ▶ G = gravitational constant ( $6.673 \times 10^{-11} \text{ m}^3/\text{s}^2\text{kg}$ )
- ▶ M = mass of the \_\_\_\_\_ body
  - Usually Earth ( $5.97 \times 10^{24} \text{ kg}$ )
- ▶ r = radius of the \_\_\_\_\_ in meters
  - Can also be distance if the information is provided as so

# Orbital Motion and Tides

## Orbital Velocity

### ▶ Ex: Moon's orbital velocity

- $G = \underline{\hspace{2cm}}$  m<sup>3</sup>/s<sup>2</sup>kg
- $M = \text{Earth}$  ( $\underline{\hspace{2cm}}$  kg)
- $r = \text{distance from the Moon to the center of Earth}$  ( $\underline{\hspace{2cm}}$ )

$$V_c = \sqrt{\frac{GM}{r}}$$

$$\begin{aligned} V_c &= \sqrt{\frac{6.67 \times 10^{-11} \times 5.97 \times 10^{24}}{3.84 \times 10^8}} = \sqrt{\frac{39.8 \times 10^{13}}{3.84 \times 10^8}} \\ &= \sqrt{1.04 \times 10^6} = 1020 \text{ m/s} = 1.02 \text{ km/s} \end{aligned}$$

# Orbital Motion and Tides

## Orbital Velocity

- ▶ Because of the velocity needed to put the \_\_\_\_\_ in orbit, large \_\_\_\_\_ are used to get them above the atmosphere and moving at a speed that sets them in that \_\_\_\_\_ orbit
- ▶ Remember, even outside of Earth's atmosphere there is still \_\_\_\_\_
  - It may be weak or pulling from another object, but it is there



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# Orbital Motion and Tides

## Escape Velocity

- ▶ **Escape Velocity** – ( $V_e$ ) the \_\_\_\_\_ required to escape from the surface of an astronomical body

$$V_e = \sqrt{\frac{2GM}{r}}$$

- ▶ Exactly like the \_\_\_\_\_ velocity formula in regards to variables
- ▶ It is just \_\_\_\_\_ times the circular velocity

# Orbital Motion and Tides

## Escape Velocity

- ▶ Ex: Escaping Earth's atmosphere

$$V_e = \sqrt{\frac{2GM}{r}}$$

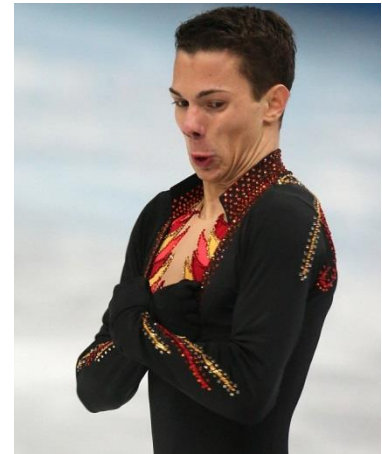
- $G = \text{_____ m}^3/\text{s}^2\text{kg}$
- $M = \text{Earth (_____ kg)}$
- $r = \text{Earth's atmosphere average radius (_____ m)}$

$$\begin{aligned} V_c &= \sqrt{\frac{2 \times 6.67 \times 10^{-11} \times 5.97 \times 10^{24}}{6.37 \times 10^6}} = \sqrt{\frac{7.96 \times 10^{14}}{6.37 \times 10^6}} \\ &= \sqrt{1.25 \times 10^8} = 11,200 \text{ m/s} = 11.2 \text{ km/s} \end{aligned}$$

# Orbital Motion and Tides

## Kepler's Laws Reexamined

- ▶ 1<sup>st</sup> law – orbits of the planets are \_\_\_\_\_ with the Sun at one focus
- ▶ 2<sup>nd</sup> law – a planet moves \_\_\_\_\_ when it is closest to the Sun and slower when it is farther away
  - **Angular momentum** – a measure of the \_\_\_\_\_ of the body about some point
    - This remains constant for planets orbiting the sun and moons that orbit planets as long as nothing speeds them up or slows them down

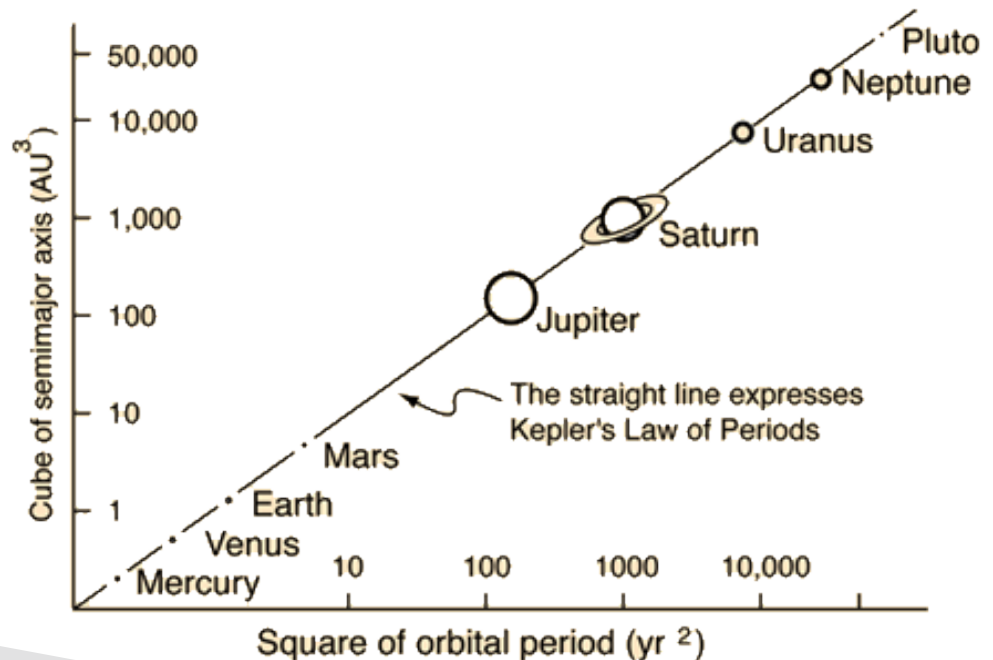




# Orbital Motion and Tides

## Kepler's Laws Reexamined

- ▶ 3<sup>rd</sup> law – planet's orbital period depends on its \_\_\_\_\_  
from the Sun
  - Relies on energy and the \_\_\_\_\_ of motion depends on how fast the planet moves
  - The gravitational attraction \_\_\_\_\_ depends on the size of orbit

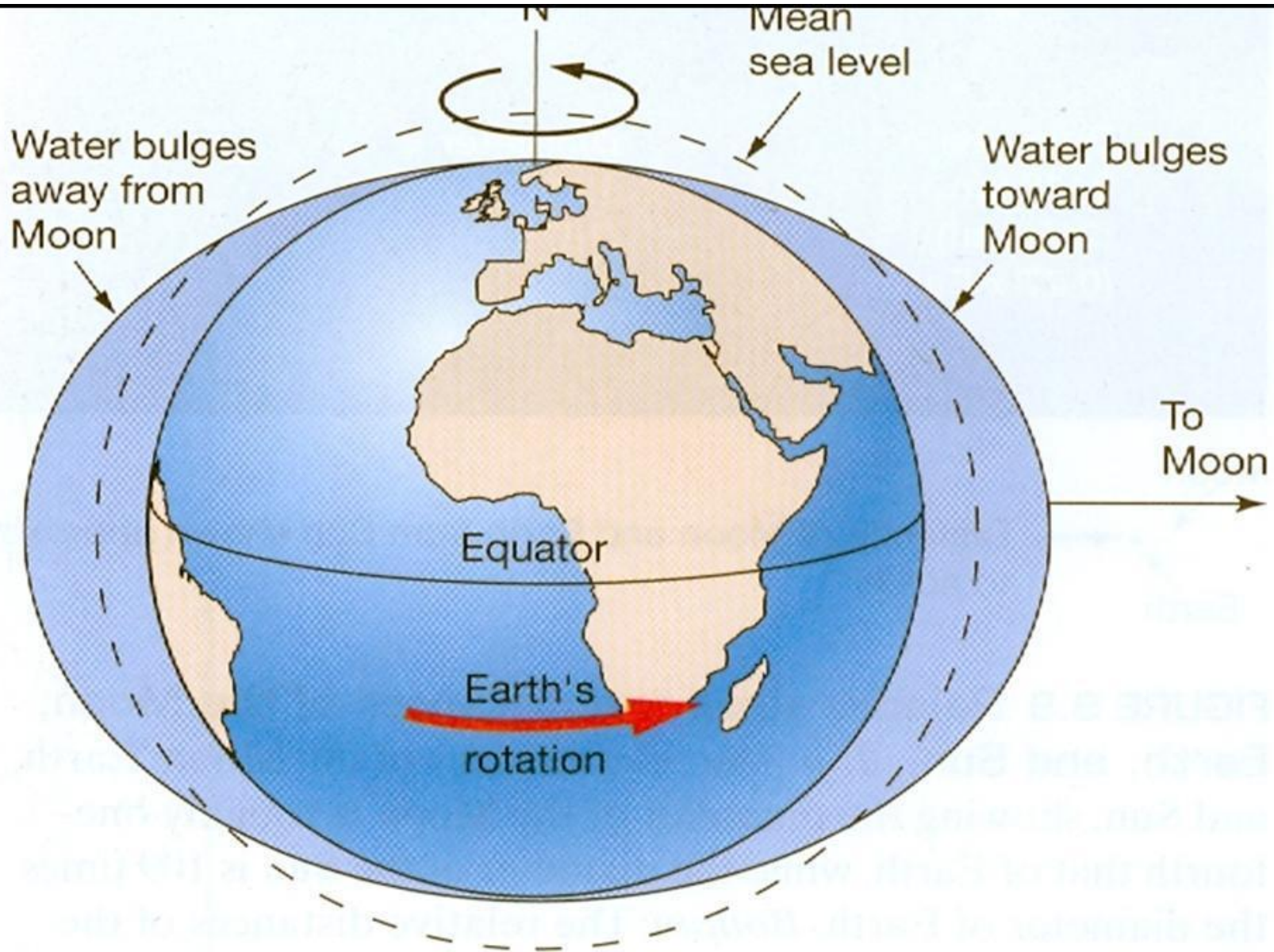


# Orbital Motion and Tides

## Tides and Tidal Forces

- ▶ Because gravity is \_\_\_\_\_ between the Earth and the Moon, the Moon's gravity can explain the ocean \_\_\_\_\_
- ▶ Tides are caused by small differences in gravitational forces
  - The pull on the side of the \_\_\_\_\_ facing the Moon causing the water to flow and bulge
  - The opposite happens on the other side of Earth at that time because it has the least \_\_\_\_\_

# Orbital Motion and Tides



# Orbital Motion and Tides

## Tides and Tidal Forces

- ▶ **Spring Tides** – tides that are \_\_\_\_\_ high and exceptionally low due to a \_\_\_\_\_ Moon/new Moon and combination with the Sun's pull
  - Yes, the Sun pulls, too, it's just not as dramatic being that it's really far away
  - “Spring” isn't season related but rather the rapid \_\_\_\_\_ in the water
- ▶ **Neap Tides** – tides that are less \_\_\_\_\_ during \_\_\_\_\_ quarter Moons because of the 90 degree angle between the Sun and Moon
  - Sun cancels out some of the Moon's pull

# Orbital Motion and Tides

